

Domain

(radicals)

① Square root fns: under radical cannot be negative

ex) $f(x) = \sqrt{x+1}$, find domain.

$$x+1 \geq 0$$

$$\underline{-1} \quad \underline{-1}$$

$$\boxed{x \geq -1}$$

$$\{x \mid x \geq -1\} \text{ "builder set"}$$

or

$$[-1, \infty)$$

ex) $f(x) = \sqrt{-x+1}$

$$-x+1 \geq 0$$

$$\underline{-1} \quad \underline{-1}$$

$$\underline{-x} \geq \underline{-1}$$

$$\underline{-1} \quad \underline{-1}$$

$$\boxed{x \leq 1}$$

$$\{x \mid x \leq 1\}$$

or

$$(-\infty, 1]$$

② Rational Fns (fractions): denominator $\neq 0$

ex) $h(x) = \frac{2}{x+3}$

$$x \neq -3 \text{ OR}$$

$$x+3 \neq 0$$

$$\underline{-3} \quad \underline{-3}$$

$$x \neq -3$$

$$\{x \mid x \neq -3\}$$

OR

$$(-\infty, -3), (-3, \infty)$$

Operations on fns

* Sum : $(f+g)(x) = f(x) + g(x)$

* Difference : $(f-g)(x) = f(x) - g(x)$

* Product : $(f \cdot g)(x) = f(x) \cdot g(x)$

* Quotient : $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} \quad g(x) \neq 0$

ex) $f(x) = x$, $g(x) = 3x - 5$

a) find $(f+g)(x) = f(x) + g(x) = x + 3x - 5$
 $= \boxed{4x - 5}$

b) find $(f-g)(x) = f(x) - g(x) = x - (3x - 5)$
 $= x - 3x + 5$
 $= \boxed{-2x + 5}$

c) find $(f \cdot g)(x) = f(x) \cdot g(x)$
 $= (x)(3x - 5)$
 $= \boxed{3x^2 - 5x}$

d) find $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x}{3x - 5}$

$$\begin{aligned} e) (f+g)(3) &= f(3) + g(3) \\ &= 3 + 3(3) - 5 \\ &= 3 + 9 - 5 \\ &= 7 \end{aligned}$$

OR

$$(f+g)(x) = 4x - 5 \text{ (from earlier)}$$

$$\begin{aligned} (f+g)(3) &= 4(3) - 5 \\ &= 12 - 5 \\ &= 7 \end{aligned}$$

