

**PRACTICE MIDTERM III**  
Part I - Calculator

1. Form a polynomial (with smallest degree possible) with the given information.

Zeros: -4 multiplicity 1, -3 multiplicity 3 and goes through the point (-2, 8).

$$f(x) = a(x+4)^1(x+3)^3$$

$$8 = a(-2+4)(-2+3)^3$$

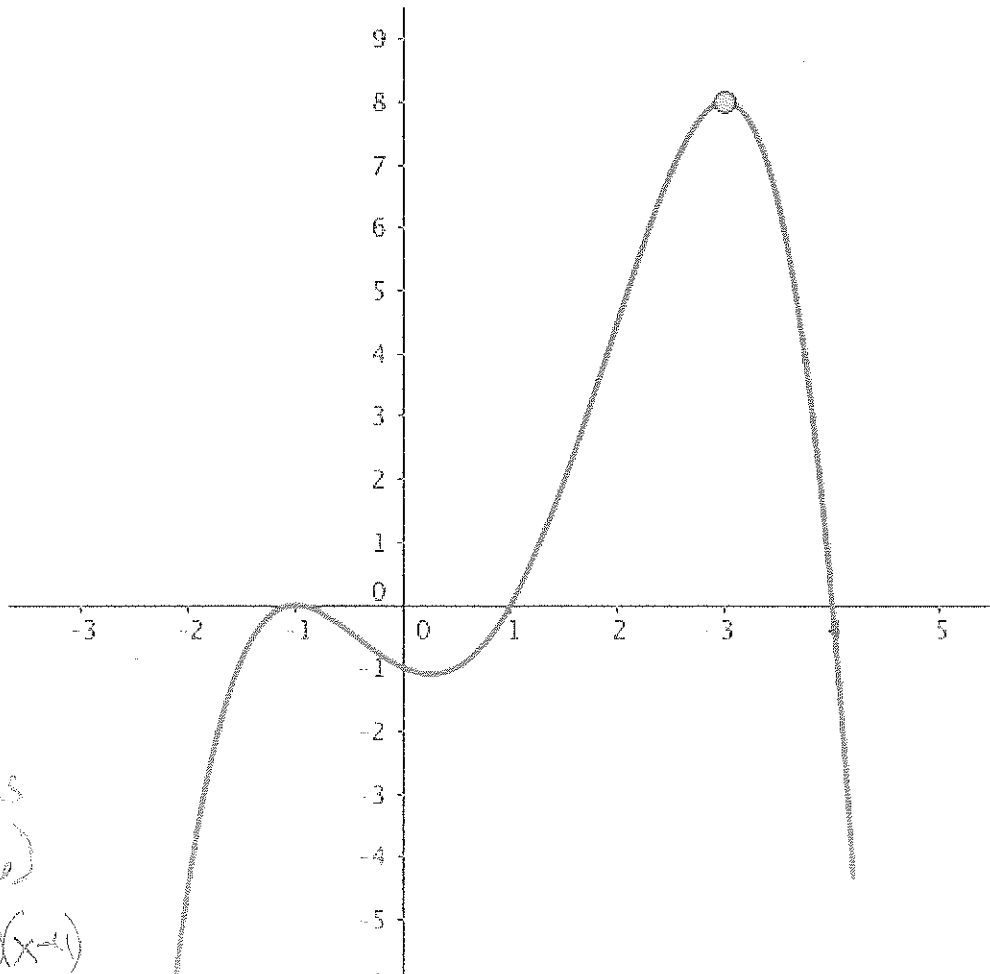
$$8 = a(2)(1)$$

$$8 = 2a$$

$$a = 4$$

$$f(x) = 4(x+4)(x+3)^3$$

2. Write a polynomial function whose graph is below. Use the smallest degree possible.



Zeros	m	+1c
-1	2	+
1	1	-
4	1	-

$$n - 1 = 3 \text{ max turns}$$

$$\therefore n = 4 \text{ (max degree)}$$

$$f(x) = a(x+1)^2(x-1)(x-4)$$

$$8 = a(3+1)^2(3-1)(3-4)$$

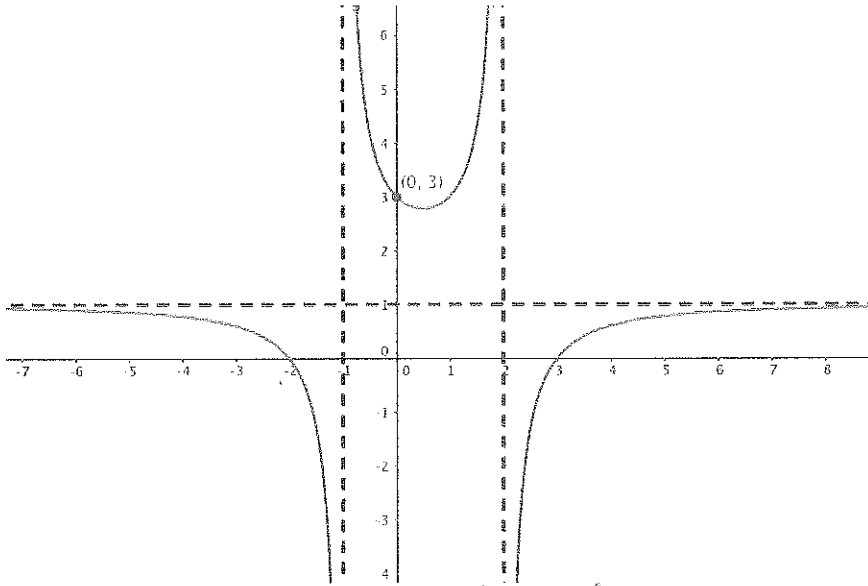
$$8 = a(16)(2)(-1)$$

$$8 = -32a$$

$$a = -\frac{1}{4}$$

$$f(x) = -\frac{1}{4}(x+1)^2(x-1)(x-4)$$

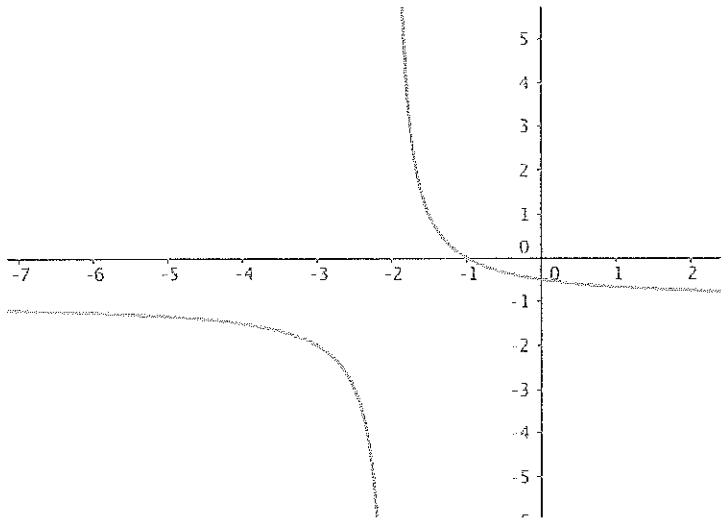
3. Find a possible formula for the graph below.



$\Rightarrow$  dicke les denom  
 VA @  $x = -1, 2$   
 NA @  $y = 1 \Rightarrow n = m$   
 zeros | m | +/c } dicke les  
       -2 | 1 | c } numerator  
       3 | 1 | c }

$$R(x) = \frac{(x+2)(x-3)}{(x+1)(x-2)}$$

4. Use knowledge of transformations to write an equation of the graph below.



$\frac{1}{x}$      $\frac{1}{x}$   
 $-\frac{1}{x}$      $-\frac{1}{x}$   
 v. shift down 1  $\Rightarrow -\frac{1}{x} - 1$   
 h. shift left by 2  $\Rightarrow -\frac{1}{(x+2)} - 1$

$$f(x) = -\frac{1}{(x+2)} - 1$$

5. State the domain, horizontal asymptote(s), and vertical asymptote(s) of  $h(x)$ .

Domain:  
 $x+1 \neq 0$      $x-3 \neq 0$   
 $x \neq -1$      $x \neq 3$

$$D: \{x \mid x \neq -1, x \neq 3\}$$

$$\begin{aligned}
 h(x) &= \frac{2(x-1)^2}{(x+1)(x-3)} \\
 \text{VA (put in reduced form)} \\
 h(x) &= \frac{2(x+1)(x-1)}{(x+1)(x-3)} \\
 &= \frac{2(x-1)}{(x-3)} \quad \text{VA @ } x=3
 \end{aligned}$$

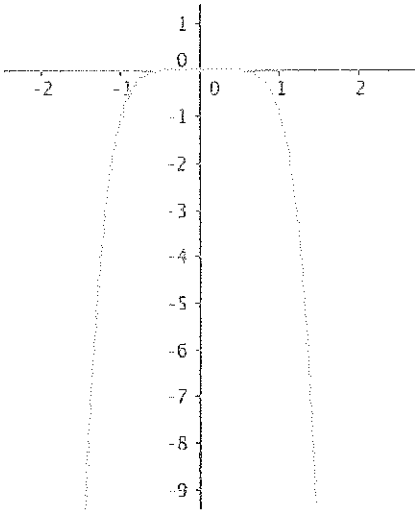
NA  
 $n = m$   
 $\therefore y = \frac{2}{1} = 2$   
 NA @  $y = 2$

**PRACTICE MIDTERM III**

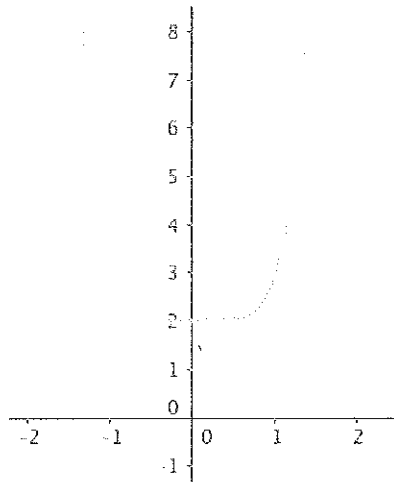
*Part II - No Calculator*

1. Match the polynomial to the graph by writing the corresponding letter beneath the graph.

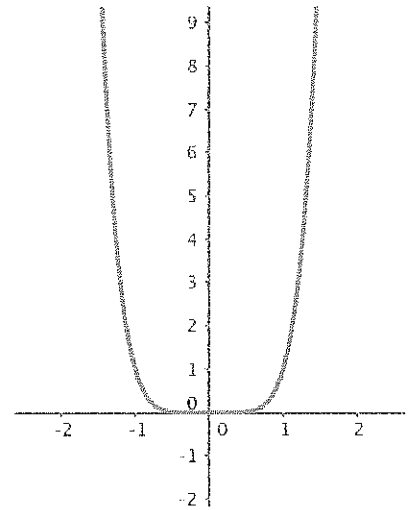
- a.  $2 - x^6$     b.  ~~$x^6 + 2$~~     c.  ~~$-x^6$~~     d.  ~~$(x - 1)^6$~~     e.  ~~$x^6$~~     f.  ~~$(x + 1)^6$~~



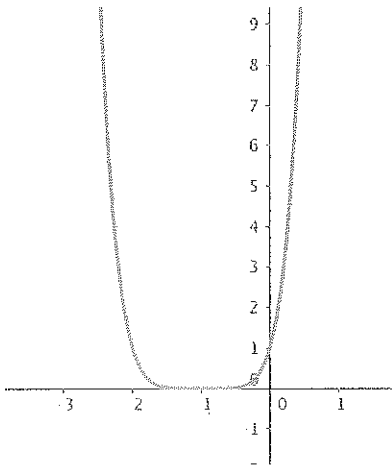
c



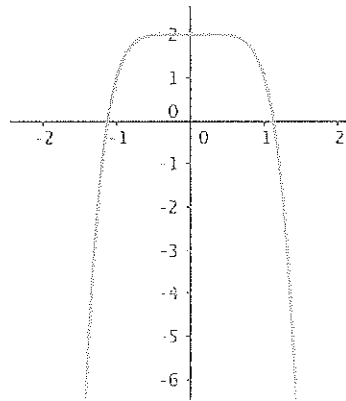
b



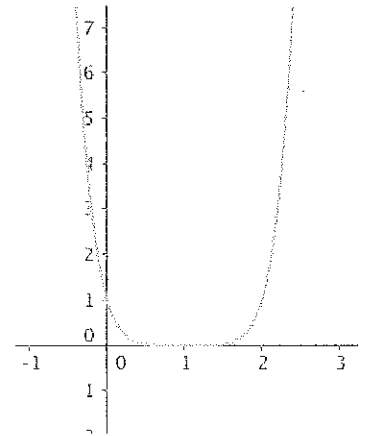
e



f



a



d

2. Analyze  $g(x)$ , as indicated below. Clearly label & respond to each step (a-e).

$$g(x) = x^2(x - 2)(x + 2)$$

- Determine the end behavior of the graph.
- Find the x- and y- intercepts of the graph of the function.
- Determine the zeros and their multiplicities. State whether the graph crosses or touches at each zero.
- Determine the maximum number of turning points on the graph of the function.
- Sketch the graph of the function.

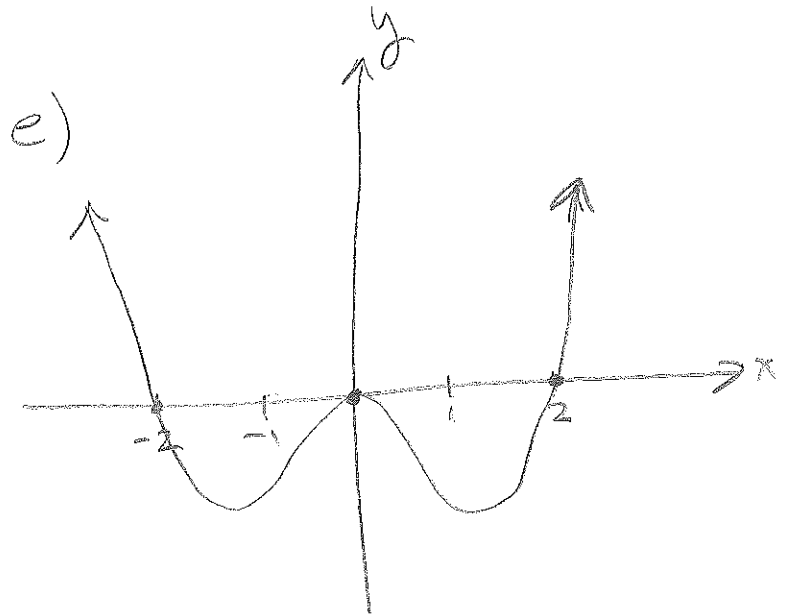
a) power function:  $x^4$   $x \rightarrow \infty, g(x) \rightarrow \infty$  "up",  $x \rightarrow -\infty, g(x) \rightarrow \infty$  "up"

b) x int when  $y = 0$   
 $x^2(x-2)(x+2) = 0$   
 $x^2 = 0$   $x-2 = 0$   $x+2 = 0$   
 $x = 0, 2, -2$

y int when  $x = 0$   
 $y = 0^2(0-2)(0+2)$   
 $y = 0$

c)

z	m	HC
0	2	+
2	1	-
-2	1	-



d) max t.p. =  $n - 1$   
 $n = \text{degree} = 4$   
 $\therefore 4 - 1 = 3$

3. Analyze  $R(x)$ , as indicated below. Clearly label & respond to each step (a-f).

$$R(x) = \frac{(x+2)(x-1)}{(x-4)(x+1)}$$

- State the domain.
- State the x- and y-intercepts of the graph.
- Find the vertical and horizontal asymptotes.
- Find the zeros, their multiplicities, and behavior (touch or cross).
- Determine intervals where the graph is above or below the x-axis.
- Graph  $R(x)$ .

a)  $(x-4)(x+1) \neq 0$   
 $x-4 \neq 0$     $x+1 \neq 0$   
 $x \neq 4, x \neq -1$

D:  $\{x \mid x \neq -4, x \neq -1\}$

b) x int when  $y=0$   
 (use numerator)  
 $(x+2)(x-1) = 0$   
 $x = -2, x = 1$

y int when  $x=0$   
 $y = \frac{(0+2)(0-1)}{(0-4)(0+1)} = \frac{-2}{-4} = \frac{1}{2}$   
 $y = \frac{1}{2}$

c) V.A. (use reduced form m + denominator)  
 $x = 4, x = -1$

H.A. ( $n=m$ )  $\therefore$  H.A. =  ~~$\frac{0}{0}$~~   
 $y = \frac{1}{1} = 1$

d)

z	m	+/c
-2	1	c
1	1	c

e) Use x-int + VA for intervals

$(-\infty, -2)$	$(-2, -1)$	$(-1, 1)$	$(1, 4)$	$(4, \infty)$
+	-	+	-	+

